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2015/2016, week 4

## **Cross-Country Income Differences**

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Romer, Chapter 1.6, 1.7, 4.2, 4.5, 4.6

# Differences in growth rates

- Verdeling van inkomen en economische groei in geïndustrialiseerde landen

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Bron: *Economen kunnen niet rekenen*

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# The power of economic growth

- Suppose China, the Netherlands and Venezuela were equivalent in terms of GDP 40 years ago
  - In 40 years, China growing 5.7 percent a year, would have become 4 times as rich as the Netherlands
  - Similarly, in 40 years time, the Netherlands would have become twice as rich as Venezuela growing 0.1 percent a year only
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# Economic growth; scope and definition

- Lecture is about structural economic growth
  - It is not about business cycle fluctuations of growth around its structural value
  - Economic growth refers to growth of the Gross Domestic Product
    - Homework
    - Environmental damage
    - Natural resources
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# Growth accounting

- Adopts the concept of the aggregate production function
  - Attributes economic growth to the contribution of different production factors
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# Growth accounting

- Consider the aggregate production function

$$Y(t) = F(K(t), A(t)L(t))$$

- Take the total derivative of the above function with respect to time:

$$\dot{Y}(t) = \frac{\partial Y(t)}{\partial K(t)} \dot{K}(t) + \frac{\partial Y(t)}{\partial L(t)} \dot{L}(t) + \frac{\partial Y(t)}{\partial A(t)} \dot{A}(t)$$

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# Growth accounting

- Dividing both sides of the equation by  $Y(t)$ , we get

$$\frac{\dot{Y}(t)}{Y(t)} = \frac{K(t)}{Y(t)} \frac{\partial Y(t)}{\partial K(t)} \frac{\dot{K}(t)}{K(t)} + \frac{L(t)}{Y(t)} \frac{\partial Y(t)}{\partial L(t)} \frac{\dot{L}(t)}{L(t)} + \frac{A(t)}{Y(t)} \frac{\partial Y(t)}{\partial A(t)} \frac{\dot{A}(t)}{A(t)}$$

- Which can be further simplified:

$$\frac{\dot{Y}(t)}{Y(t)} = \alpha_K(t) \frac{\dot{K}(t)}{K(t)} + \alpha_L(t) \left[ \frac{\dot{L}(t)}{L(t)} + \frac{\dot{A}(t)}{A(t)} \right]$$

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# Growth accounting

- Given that we have CRS,  $\alpha_K(t) = 1 - \alpha_L(t)$ , we have the growth accounting equation:

$$\frac{\dot{Y}(t)}{Y(t)} = \frac{\dot{L}(t)}{L(t)} + \alpha_K(t) \left[ \frac{\dot{K}(t)}{K(t)} - \frac{\dot{L}(t)}{L(t)} \right] + (1 - \alpha_K(t)) \frac{\dot{A}(t)}{A(t)}$$

- An alternative formula is the following:

$$\frac{\dot{Y}(t)}{Y(t)} - \frac{\dot{L}(t)}{L(t)} = \alpha_K(t) \left[ \frac{\dot{K}(t)}{K(t)} - \frac{\dot{L}(t)}{L(t)} \right] + R(t)$$

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# Growth accounting

- According to the growth accounting equation, economic growth is attributed to
    - Growth in the input of labour
    - Growth in the input of physical capital
    - The Solow residual:
      - Technological progress
      - All other elements
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## Empirical application

- Interesting application is Young (1995)
  - He adopts technique of growth accounting to explain the extraordinary postwar growth of Hong Kong, Singapore, South Korea and Taiwan (Newly Industrializing Economies)
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## Empirical application

- Result: economic growth has been high due to
    - Rising investment rates
    - Increasing labour force participation rates
    - Increasing levels of education
    - Intersectoral reallocations of labour towards the non-agricultural and manufacturing sector
  - Additionally, the contribution of other factors such as total factor productivity growth has been limited
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## Growth accounting: caveat

- The factors that, according to growth accounting, drive economic growth, may be dependent on one another
  - For example,
    - Labour force participation and education may both be related to labour productivity growth
    - Capital accumulation and also labour force participation may depend on technological progress
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## Growth accounting: caveat

- Hence, the technique of growth accounting may overstate or understate the contribution of a factor of production
  - For example, suppose  $A(t)$  increases with one percent
    - According to growth accounting, this increases GDP with  $(1 - \alpha_K(t))$  percent
    - If capital accumulation increases upon an increase in the level of technology, the growth effect is higher
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## Growth accounting: caveat

- Growth accounting can thus be used for linking economic growth to different factors of production
  - Growth accounting should thus not be used for 'what if' simulation analysis
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## The Solow Growth model: the balanced growth path

- Along the balanced growth path,  $Y/L$  and  $K/L$  grow at rate  $g$
  - But  $g$  is exogenous
  - So the Solow model describes long-run growth by just imposing it!
  - In addition, the model is very abstract as regards the description of knowledge (or effectiveness of labour)
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## The Solow Growth model: convergence

- The Solow Growth model predicts convergence to a state of balanced growth
  - Hence, countries starting below their long-run paths grow faster than those starting above
  - To see that consider a case where differences in  $Y/L$  stem only from physical capital per worker  $K/L$ . That is, human capital per worker and output for given inputs are the same across countries
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## The Solow Growth model: convergence

- Assume again the CRS production function

$$Y(t) = F(K(t), A(t)L(t))$$

- Recall the adjustment equation for capital per effective worker:

$$\dot{k} = \lambda \left[ k_i^* - k_i(t) \right]$$

- $\lambda > 0$  measures the rate of convergence
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## The Solow Growth model: convergence

- This says that the farther is the economy below its balanced growth path, the faster does  $K/L$  grow
  - For  $Y/L$  a similar expression applies
  - Hence, also  $Y/L$  grows faster the more  $Y/L$  differs from its steady-state level
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## The Solow Growth model: convergence

- ❑ As to the value of  $k^*$ , one can make two alternative assumptions
  - ❑ One is that  $k^*$  is the same in all countries
    - ❑ In this case, all countries grow towards the same  $Y/L$
    - ❑ The lower is the initial level  $Y/L$ , the faster is the growth of  $Y/L$
    - ❑ We call this *unconditional convergence*
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## The Solow Growth model: convergence

- A second assumption is that  $k^*$  varies across countries
    - In this case, there is a persistent component of cross-country income differences
    - Poor countries (e.g., with low saving rates) may not grow faster than other countries
    - There is still convergence towards the own balanced growth path
    - We call this *conditional convergence*
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## The Solow Growth model: convergence

- Unconditional convergence gives a good description of differences in growth among industrialized countries in the post-war period
    - This is so since saving rates, levels of education and other factors related to long-run fundamentals are similar across industrialized countries
  - For the same reason, it does not work that well for countries all over the world
    - In terms of the Solow Growth model,  $s$ ,  $n$  and  $g$  can differ a lot between countries
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# Differences in growth rates

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## Estimating convergence

- Baumol (1986) addresses the question whether the growth performance of countries features convergence
- Baumol (1986) examines convergence from 1870 to 1979 among 16 industrialized countries
  - He regresses output growth over this period on a constant and initial income
  - Model specification:

$$\ln \left[ \left( \frac{Y}{N} \right)_{i,1979} \right] - \ln \left[ \left( \frac{Y}{N} \right)_{i,1870} \right] = a + b \ln \left[ \left( \frac{Y}{N} \right)_{i,1870} \right] + \varepsilon_i$$

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## Estimating convergence

- $\ln(Y/N)$  is log income per person,  $\varepsilon$  is an error term, and  $i$  indexes countries
  - Convergence if  $b < 0$ : countries with higher initial incomes have lower growth
  - Perfect convergence if  $b = -1$
  - No convergence if  $b = 0$
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# Estimating convergence

- Estimation result:

$$\ln \left[ \left( \frac{Y}{N} \right)_{i,1979} \right] - \ln \left[ \left( \frac{Y}{N} \right)_{i,1870} \right] = 8.457 - \underset{(0.094)}{0.995} \ln \left[ \left( \frac{Y}{N} \right)_{i,1870} \right],$$

$$R^2 = 0.87, \quad \text{s.e.e.} = 0.15,$$

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## Estimating convergence

- DeLong (1988) shows that Baumol's finding is largely spurious, due to
  - Sample selection:
    - since historical data are constructed retrospectively, the countries that have long data series are generally those that are the most industrialized today
  - Measurement error:
    - estimates of real income per capita in 1870 are imprecise. Measurement error creates bias toward finding convergence
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## Estimating convergence

- One way to tackle the first problem is to increase the sample and compare the richest countries as of 1870
  - DeLong (1988) creates a sample that consists of all countries at least as rich as the second poorest country in Baumol's sample in 1870, Finland
  - Hence, he adds 7 countries (Argentina, Chile, East Germany, Ireland, New Zealand, Portugal, and Spain) and drops one (Japan)
  - Result:
    - the estimate of  $b$  of  $-0.995$  drops to  $-0.566$  and becomes less statistically significant
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## Estimating convergence

- Way to tackle the second problem (i.e. measurement error) is to estimate:

$$\ln \left[ \left( \frac{Y}{N} \right)_{i,1979} \right] - \ln \left[ \left( \frac{Y}{N} \right)_{i,1870} \right]^* = a + b \ln \left[ \left( \frac{Y}{N} \right)_{i,1870} \right]^* + \varepsilon_i,$$

$$\ln \left[ \left( \frac{Y}{N} \right)_{i,1870} \right] = \ln \left[ \left( \frac{Y}{N} \right)_{i,1870} \right]^* + u_i.$$

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## Estimating convergence

- $\ln[(Y/N)1870]^*$  is the true value of log income per capita in 1870
  - $\ln[(Y/N)1870]$  is the measured value
  - $\varepsilon$  and  $u$  are assumed to be uncorrelated with each other and with  $\ln[(Y/N)1870]^*$
  - Result:
    - depending on the guess for the standard deviation of the estimation error, the estimate for  $b$  drops further, to 0 or even 1, thereby eliminating all of the remainder of Baumol's estimate of convergence
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## Cross-country income differences: the role of capital

- Where do income differences (i.e., differences in  $Y/L$ ) between countries stem from?
  - Similarly, what makes income differ between time periods?
  - According to the Solow model, there are two candidate factors:
    - Differences in the capital per worker ( $K/L$ )
    - Differences in the effectiveness of labour ( $A$ )
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## Cross-country income differences: the role of capital

- Take the production function. This reads as follows:
    - $Y = F(K, AL) \quad \rightarrow \quad y = F(k, A)$
    - Where  $y$  and  $k$  are defined as output and capital respectively per worker (!):
    - $y = \frac{Y}{L}; k = \frac{K}{L}$
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## Cross-country income differences: the role of capital

- Assume the production function is Cobb-Douglas:
    - $Y = K^\alpha (AL)^{1-\alpha} \rightarrow$
    - $y = k^\alpha A^{1-\alpha}$
  - Income difference between countries A and B:
    - $y = k^\alpha A^{1-\alpha}$
    - $\left(\frac{y^A}{y^B}\right) = \left(\frac{k^A}{k^B}\right)^\alpha \left(\frac{A^A}{A^B}\right)^{1-\alpha}$
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## Cross-country income differences: the role of capital

- Can differences in the stocks of capital per worker explain income differences between countries?
- In order to account for the difference in income between a rich country and a poor country of a factor 10, the stocks of capital need to differ a factor  $(10)^{1/\alpha}$

- Formally, solve  $\left(\frac{y^A}{y^B}\right) = 10 = \left(\frac{k^A}{k^B}\right)^\alpha \rightarrow$   
 $\left(\frac{k^A}{k^B}\right) = (10)^{1/\alpha}$



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## Cross-country income differences: the role of capital

- Standard elasticity of output w.r.t. capital
  - $\alpha = 1/3: \left(\frac{k^A}{k^B}\right) = (10)^{1/(\frac{1}{3})} = 1000$
  - Elasticity using broad measure of capital
  - $\alpha = 1/2: \left(\frac{k^A}{k^B}\right) = (10)^{1/(\frac{1}{2})} = 100$
  - Capital stocks differ not more than a factor 20 to 30 between rich and poor countries
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## Cross-country income differences: the role of capital

- The marginal product of capital in the Cobb-Douglas case:
    - $y = f(k) = k^\alpha \quad \rightarrow$
    - $f'(k) = \alpha k^{\alpha-1} = \alpha y^{(\alpha-1)/\alpha}$
  - In order to account for the difference in income between a rich country and a poor country of a factor 10, the marginal products of capital differ a factor  $(10)^{(\alpha-1)/\alpha}$
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## Cross-country income differences: the role of capital

- Standard elasticity of output w.r.t. capital
  - $\alpha = 1/3: \left( \frac{f'(k)^A}{f'(k)^B} \right) = (10)^{(-2/3)/(1/3)} = 0.01$
  - Elasticity using broad measure of capital
  - $\alpha = 1/2: \left( \frac{f'(k)^A}{f'(k)^B} \right) = (10)^{(-1/2)/(1/2)} = 0.1$
  - Rates of return do not differ a factor 10 or 100 between countries
  - If they did so, we would observe massive capital flows from rich to poor countries
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## Income differences over time: the role of capital

- For differences in income over time, the same holds true as for differences in income between countries:
    - In the data, capital stocks and rate of return on capital do not differ enough to account for the output differences
  - This implies
    - That countries and time periods differ a lot in terms of  $A$
    - Or, that capital is much more valuable than is reflected in its price
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## Cross-country income differences: human capital

- How about extending the approach by including human capital?
- Would that increase the contribution from capital (and decrease the role of technology or, better, the residual)?
- Take the following Cobb-Douglas production function

$$Y(t) = K(t)^a (A(t)H(t))^{1-a}$$

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## Cross-country income differences: human capital

- One can think of human capital  $H$  as the contribution of skills, expertise or education to the quality of labour
  - The more educated, skilled or experienced the labour force, the higher is human capital  $H$
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## Cross-country income differences: human capital

- To see how the introduction of human capital improves the ability of the model to explain income per capita growth and, hence, cross-country income differences, consider our new production function (in per capita terms) in logs

$$\ln \frac{Y_i}{L_i} = a \ln \frac{K_i}{L_i} + (1 - a) \ln \frac{H_i}{L_i} + (1 - a) \ln A_i$$

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## Cross-country income differences: human capital

- The above equation can be further rearranged as

- $\ln \frac{Y_i}{L_i} = \frac{a}{1-a} \ln \frac{K_i}{Y_i} + \ln \frac{H_i}{L_i} + \ln A_i$



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## Cross-country income differences: human capital

- Empirical Results; the hard part is to find a good proxy for the human capital term  $H$ 
    - In empirical studies, it is proxied with years of schooling
  - Hall & Jones (1999) compare the five richest countries in their sample with the five poorest ones
  - Average  $Y/L$  in the rich group exceeds that in the poor group by 31.7 (or 3.5 in logs)
  - The contribution of  $(a/(1-a))\ln(K/Y)$  is 0.6, that of  $\ln(H/L)$  is 0.8, and that of  $\ln(A)$  is 2.1
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## Cross-country income differences: human capital

- That is, only about a sixth in the gap between the richest countries and the poorest ones is due to differences in physical capital intensity
  - Only a slightly larger fraction is due to differences in schooling
  - The largest part of country differences in income per capita is due to differences in technology or other factors included in the Solow residual
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# Cross-country income differences: human capital

- Extensions:

- Human capital also depends on nationality worker (Klenow and Rodríguez-Claire 1997, Hendricks 2002)
- Return to education may be different for different types of education
- Low-skilled labour and high-skilled labour may be complements in production

- Conclusion does not change:

- The inclusion of human capital into the production function does not lead to dramatically different results
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## Cross-country income differences: the residual $A$

- The fact that the residual term  $A$  is not well defined makes the empirical analysis tough. Why?
  - Because we want to know the determinants of growth.
    - What are the determinants of economic growth?
    - Are they exogenous or endogenously related to economic policies?
    - If so, which kind of economic policies?
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## Cross-country income differences: the residual A

- ❑ A bunch of other possible factors exist that can contribute to an explanation of economic growth
  - ❑ Charles Jones introduced the term social infrastructure
    - ❑ The whole of government activities that impact on the wedge between social and private returns
    - ❑ The definition is very broad: the activities may increase or deteriorate social welfare
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# Cross-country income differences: social infrastructure

- Taxation and subsidization of various activities (labour supply, saving, investment, education)
    - Operational costs
    - Costs in terms of changed economic behaviour
    - Costs in terms of an expansion of the informal economy
  - Legislation
    - Crime
    - Enforceability of contracts
  - Government expropriation, bribery
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# Cross-country income differences: social infrastructure

- ❑ Values and norms
    - ❑ Religion
    - ❑ Individual initiative
  - ❑ Interest groups
    - ❑ Dictatorship
    - ❑ Bribe-taking officials
    - ❑ Firms that benefit from a lack of competition
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## Cross-country income differences: geography

- ❑ Average incomes in countries within 20 degrees of the equator are less than a sixth of those in countries at more than 40 degrees of latitude
  - ❑ The former countries feature environments more conducive to disease
  - ❑ The former countries feature climates less favourable to agriculture
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## Cross-country income differences: colonization strategies

- ❑ Acemoglu, Johnson and Robinson argue that today's institutions – which are important for economic growth – have been shaped by colonization strategies as pursued by European countries in the past few centuries
  - ❑ 1 Establishment of “extractive states” that focus on exploitation without creating democratic institutions in high-mortality regions (Latin American countries)
  - ❑ 2 Establishment of “settler colonies” that create institutions similar to those in the colonist countries in low-mortality regions (United States, Australia, New Zealand)
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## Cross-country income differences: colonization strategies

- ❑ Acemoglu and Robinson (2012), *Why Nations Fail*
    - The origins of power, prosperity and poverty
  - ❑ Book blends economics, politics and history
  - ❑ Argues that economic growth stems from inclusive institutions
  - ❑ On the contrary, extractive institutions hinder economic growth
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## Cross-country income differences: the residual A

- ❑ The precise role of all these factors is still unknown, but currently widely investigated
  - ❑ Economists may fail to ever produce definitive answers to the question of the ultimate determinants of economic growth on account of
    - ❑ a lack of empirical data
    - ❑ a lack of social experiments
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